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17MATDIP41

Fourth Semester B.E. Degree Examination, Feb./Mar. 2022 Additional Mathematics - II

Time: 3 hrs .
Max. Marks: 100

## Note: Answer any FIVE full questions, choosing ONE full question from each module.

## Module-1

1 a. Find the rank of the matrix by elementary row transformation:

$$
\left[\begin{array}{llll}
1 & 2 & 3 & 2 \\
2 & 3 & 5 & 1 \\
1 & 3 & 4 & 5
\end{array}\right]
$$

b. Solve the following system of linear equations by Gauss elimination method:
$\mathrm{x}+\mathrm{y}+\mathrm{z}=9 ; \quad \mathrm{x}-2 \mathrm{y}+3 \mathrm{z}=8 ; \quad 2 \mathrm{x}+\mathrm{y}-\mathrm{z}=3$
(07 Marks)
c. Find the eigen values and eigen vectors of the matrix $\left[\begin{array}{cc}1 & -2 \\ -5 & 4\end{array}\right]$. OR
2 a. Find the rank of the matrix by elementary row transformation

$$
\left[\begin{array}{lll}
1 & 2 & 3 \\
1 & 4 & 2 \\
2 & 6 & 5
\end{array}\right]
$$

(06 Marks)
b. Use Cayley-Hamilton theorem to find the inverse of $\mathrm{A}=\left[\begin{array}{ccc}2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2\end{array}\right]$.
c. Test for consistency and solve $\mathrm{x}+\mathrm{y}+\mathrm{z}=6, \quad \mathrm{x}-\mathrm{y}+2 \mathrm{z}=5, \quad 3 \mathrm{x}+\mathrm{y}+\mathrm{z}=8$.
(07 Marks)

## Module-2

3 a. Solve $\left(D^{3}-2 D^{2}+4 D-8\right) y=0$ where $D=\frac{d}{d x}$.
(06 Marks)
b. Solve $\left(6 D^{2}+17 D+12\right) y=e^{-x}$, where $D=\frac{d}{d x}$
(07 Marks)
c. Solve $\left(D^{2}+a^{2}\right) y=$ secax by the method of variation of parameters.
(07 Marks)

## OR

4 a. Solve $\left(D^{3}-3 D+2\right) y=0$ where $D=\frac{d}{d x}$.
(06 Marks)
b. Solve $\left(D^{2}-4 D+13\right) y=\cos 2 x$ where $D=\frac{d}{d x}$.
(07 Marks)
c. Solve $\left(D^{2}+2 D+1\right) y=2 x+x^{2}$ where $D=\frac{d}{d x}$.

## Module-3

5 a. Find the Laplace transform of the function $\mathrm{L}\left\{\mathrm{e}^{-2 \mathrm{t}}(2 \cos 5 \mathrm{t}-\sin 5 \mathrm{t})\right\}$.
(06 Marks)
b. Find the Laplace transform of the function $L\{t \cdot \cos a t\}$.
(07 Marks)
c. If $\mathrm{f}(\mathrm{t})=\mathrm{t}^{2}, 0<\mathrm{t}<2$, and $\mathrm{f}(\mathrm{t}+2)=\mathrm{f}(\mathrm{t})$, for $\mathrm{t}>2$, find $\mathrm{L}\{\mathrm{f}(\mathrm{t})\}$
(07 Marks)

## OR

6 a. Find the Laplace transform of the function $L\left\{e^{3 t} \sin 5 t \sin 3 t\right\}$.
(06 Marks)
b. Find the Laplace transform of $\frac{\mathrm{e}^{-a t}-\mathrm{e}^{-\mathrm{bt}}}{\mathrm{t}}$.
(07 Marks)
c. Find the Laplace transform of the function $L\left\{3 t^{2}+4 t+5\right\} . u(t-3)$.
(07 Marks)

## Module-4

7 a. Find the inverse Laplace transform of the function $\left\{\frac{1}{s+2}+\frac{3}{2 s+5}-\frac{4}{3 s-2}\right\}$.
(06 Marks)
b. Find the inverse Laplace transform of the function $\frac{3 s+2}{(s-2)(s+1)}$.
(07 Marks)
c. Solve by using Laplace transforms $\frac{\mathrm{d}^{2} \mathrm{y}}{\mathrm{dt}^{2}+\mathrm{K}^{2} \mathrm{y}=0}$ given that $\mathrm{y}(0)=2, \mathrm{y}^{\prime}(0)=0$.
(07 Marks)

## OR

8 a. Find the inverse Laplace transform of the function $\left\{\frac{s+2}{s^{2}+36}+\frac{4 s-1}{s^{2}+25}\right\}$.
(06 Marks)
b. Find the inverse Laplace transform of the function $\frac{s+2}{s^{2}(s+3)}$.
(07 Marks)
c. Solve $\frac{d^{2} y}{d t^{2}}+4 \frac{d y}{d t}+4 y=e^{-t}, y(0)=0, y^{\prime}(0)=0$ by using Laplace transform method.
(07 Marks)

## Module-5

9 a. A bag contains 7 white, 6 red and 5 black balls, two balls are drawn at random. Find the probability that they will both be white.
(06 Marks)
b. If $A$ and $B$ are any two events, then prove that $P(A \cup B)=P(A)+P(B)-P(A \cap B)$.
c. State and prove Bayee's theorem.
(07 Marks)
(07 Marks)

## OR

10 a. A has 2 shares in a lottery in which there are 3 prizes and 5 blanks; B has 3 shares in a lottery in which there are 4 prizes and 6 blanks. Show that A's chance of success is to B's as 27:35.
(06 Marks)
b. A card is drawn from a well-shuffled pack of playing cards. What is the probability that it is either a spade or an ace?
(07 Marks)
c. A bag X contains 2 white and 3 red balls and a bag Y contains 4 white and 5 red balls. One ball is drawn at random from one of the bags and is found to the red. Find the probability that it was drawn from bag Y.
(07 Marks)

